

Self-configuring photonics – circuits, architectures, topologies and algorithms

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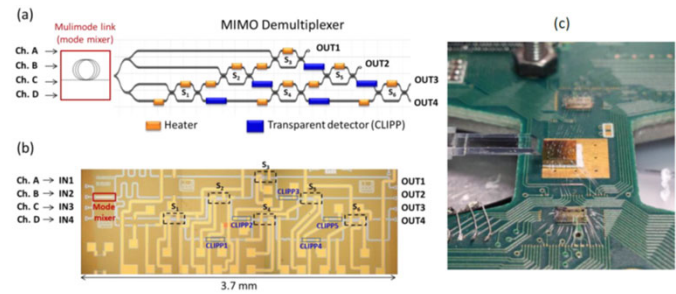
Introduction

In recent years, we have discovered architectures and algorithms that

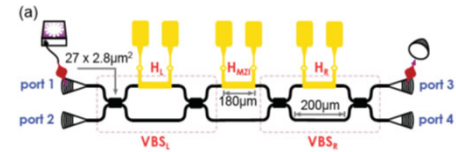
- allow control and programming of complex photonic circuits
- automatically self-configure and self-stabilize
- including adapting to problems that change in time

with many potential applications, e.g.,

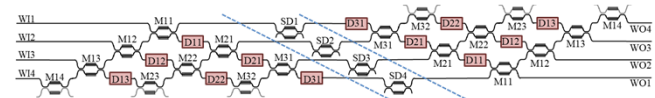
- communications
- information processing
- sensing



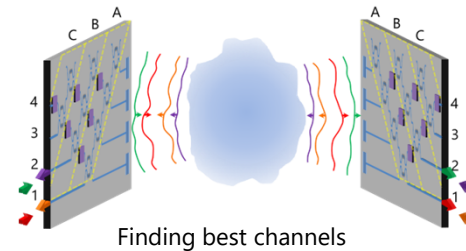
Automatic separation of mixed modes



Perfect optics from imperfect components



Universal SVD architecture for matrix multiplications



Finding best channels

Introduction

New mathematical and physical descriptions now support these new kinds of optical systems

a new topological understanding and associated algorithms

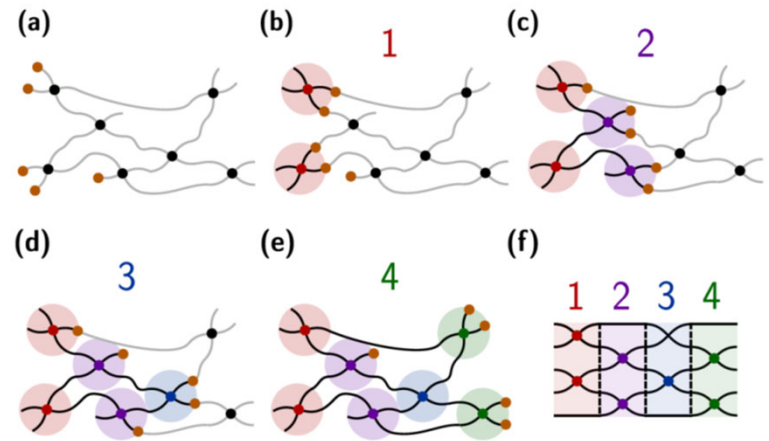
a new, "modal" view of optics

beyond conventional resonator and propagating modes

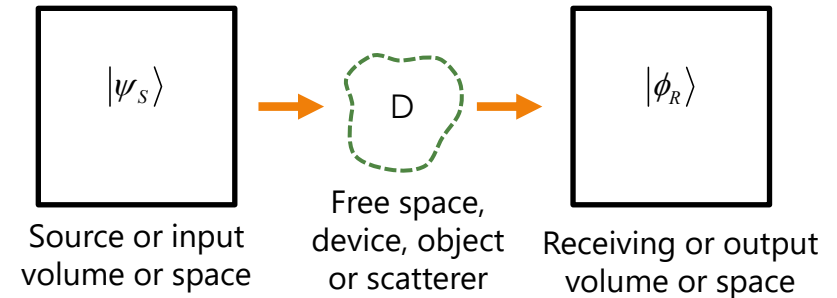
and even classic "beams"

This new "modal" approach is also fundamentally important in optics

mapping well to these new circuits as well as previous optics



S. Pai, I. A. D. Williamson, T. W. Hughes, M. Minkov, O. Solgaard, S. Fan, and D. A. B. Miller, "Parallel programming of an arbitrary feedforward photonic network," IEEE J. Sel. Top. Quantum Electron. 25, 6100813 (2020)



D. A. B. Miller, "Waves, modes, communications, and optics: a tutorial," Adv. Opt. Photon. 11, 679-825 (2019)

Summary

Introduce ideas of

programmable, self-configuring, and self-stabilizing complex interferometric circuits
and first areas of applications being explored

Briefly introduce the new “modal” way of looking at optics

which also helps us understand these systems and what they can do

For a broad review of such circuits see

W. Bogaerts et al., "Programmable photonic circuits,"
Nature 586, 207 (2020)

**For understanding the new modal approach to
optics see**

D. Miller, "Waves, modes, communications, and
optics: a tutorial," Adv. Opt. Photon. 11, 679 (2019)

A simple self-configuring circuit – the self-aligning beam coupler

Nulling a Mach-Zehnder output

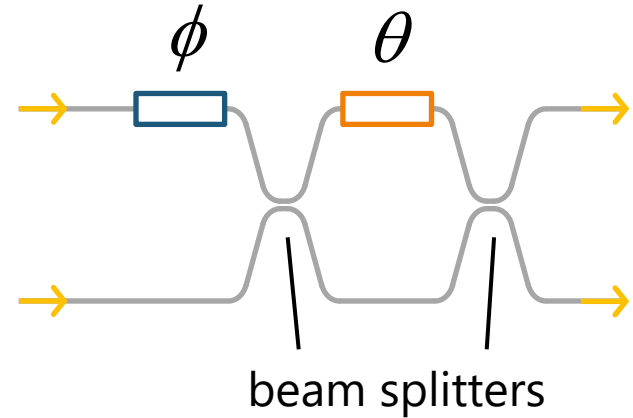
Consider a waveguide Mach-Zehnder interferometer (MZI)

formed from two "50:50" beam splitters

and at least two phase shifters

one, ϕ , to control the relative phase of the two inputs

a second, θ , to control the relative phase on the interferometer "arms"



Nulling a Mach-Zehnder output

In such an MZI with 50:50
beamsplitters

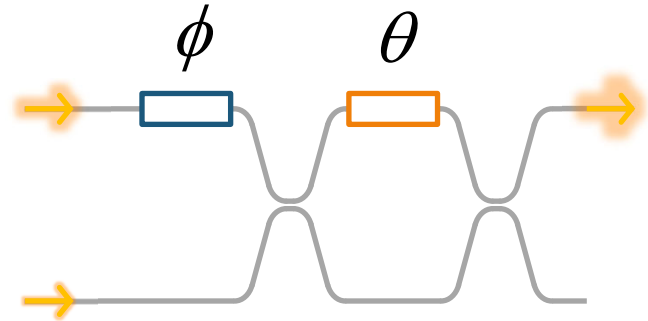
for any relative input amplitudes and
phases

we can “null” out the power at the
bottom output

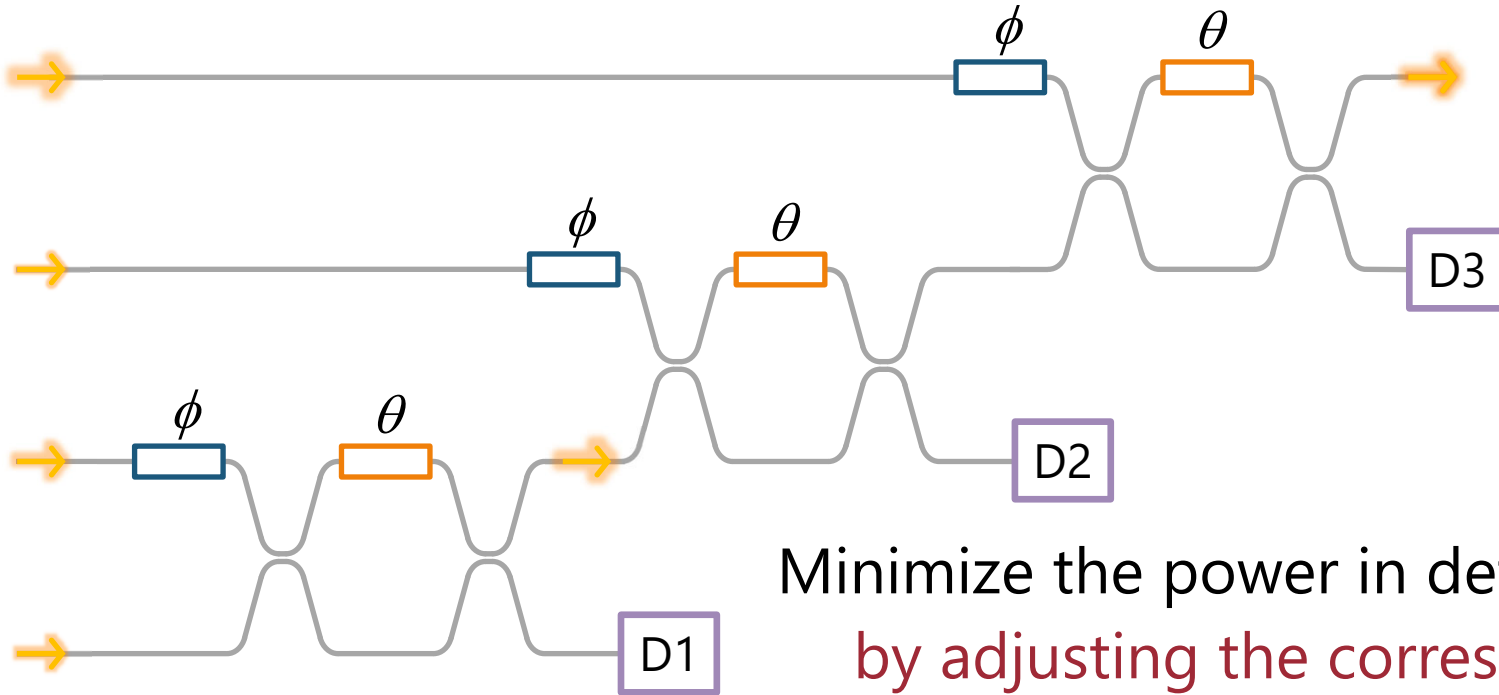
by two successive single-
parameter power minimizations

first, using ϕ

second, using θ



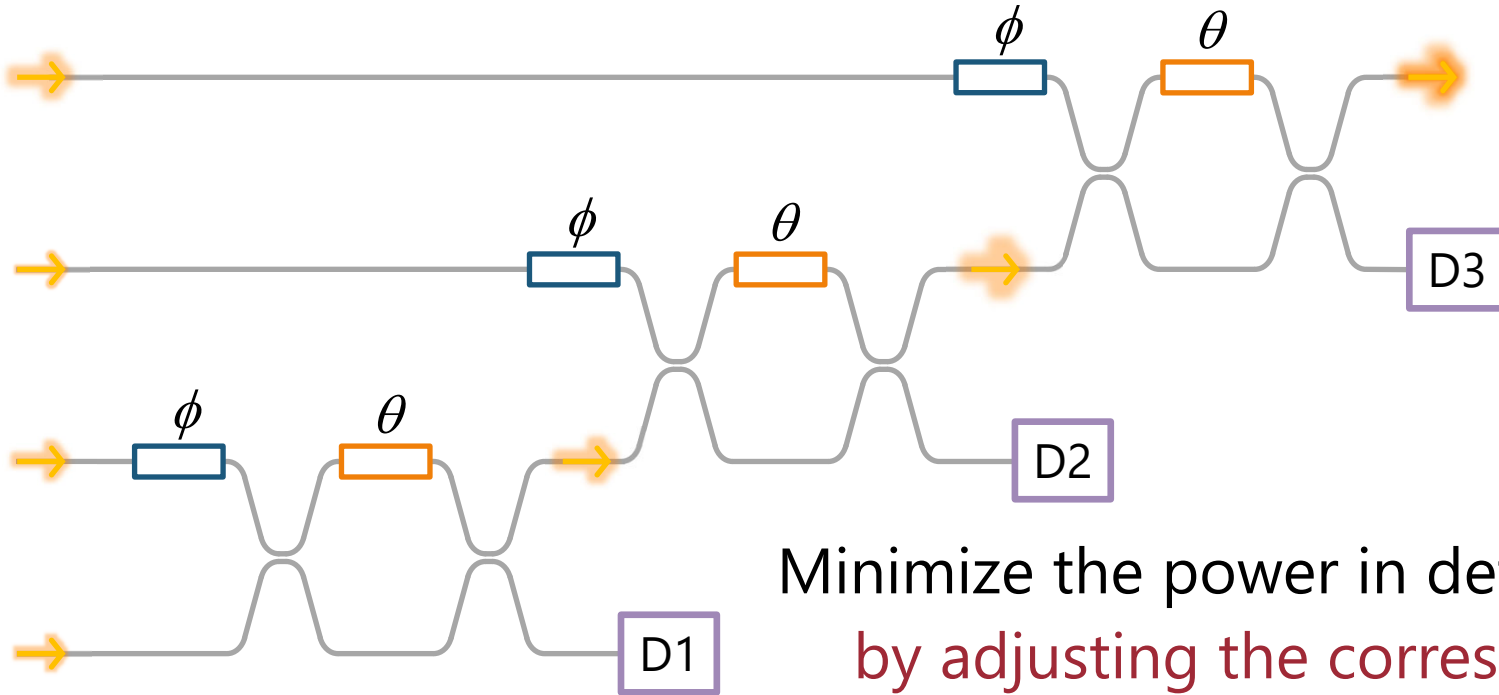
"Diagonal line" self-aligning coupler



"Self-aligning universal
beam coupler," Opt. Express
21, 6360 (2013)

Minimize the power in detector D1
by adjusting the corresponding ϕ
and then θ
putting all power in the upper output

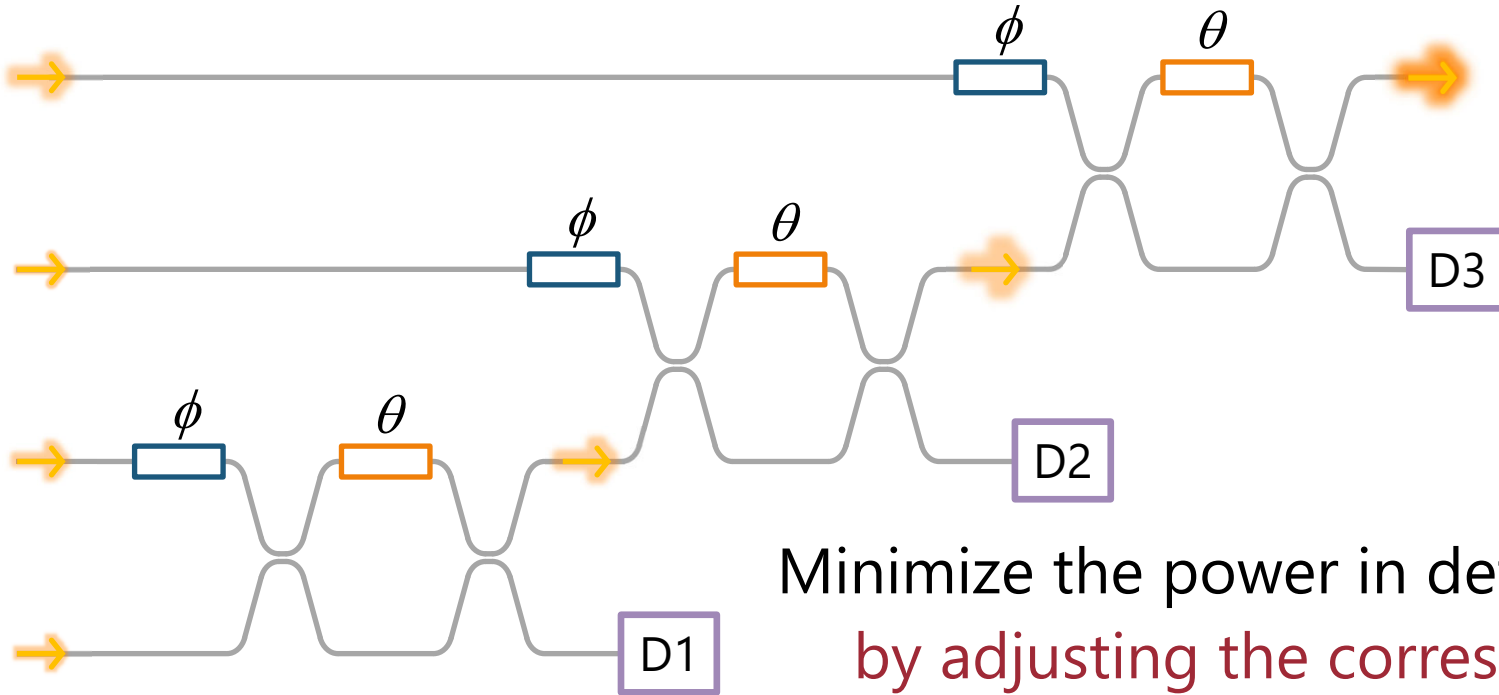
"Diagonal line" self-aligning coupler



"Self-aligning universal beam coupler," Opt. Express **21**, 6360 (2013)

Minimize the power in detector D2
by adjusting the corresponding ϕ
and then θ
putting all power in the upper output

"Diagonal line" self-aligning coupler



"Self-aligning universal beam coupler," Opt. Express **21**, 6360 (2013)

Minimize the power in detector D3
by adjusting the corresponding ϕ
and then θ
putting all power in the upper output

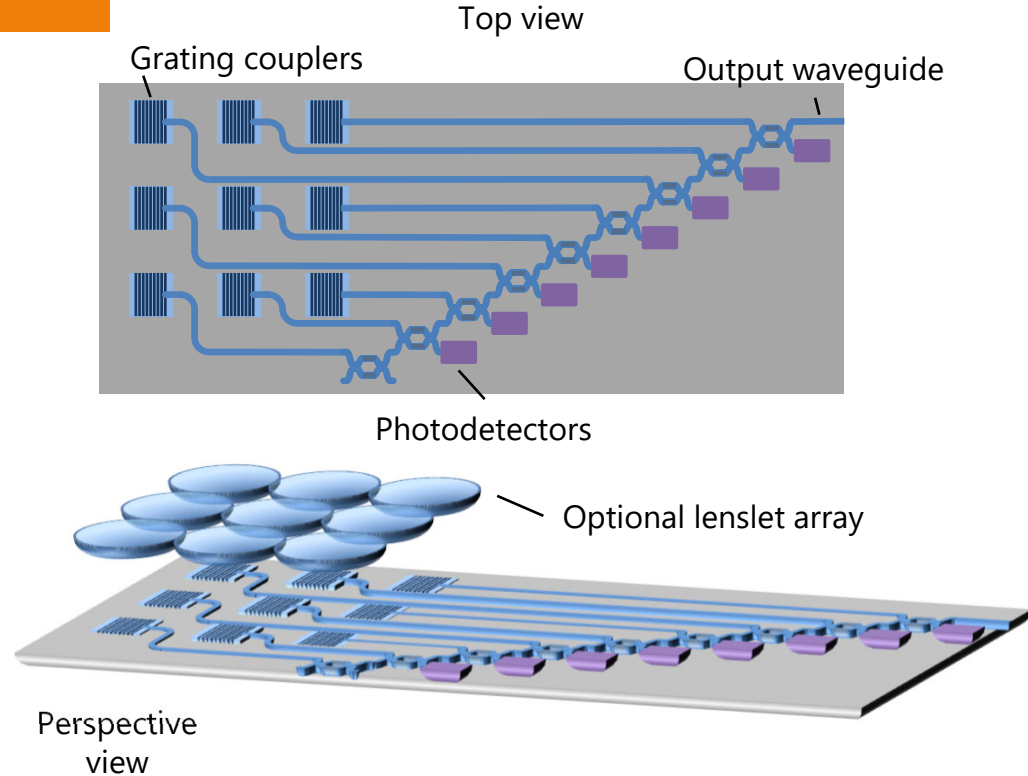
Self-aligning beam coupler

Grating couplers could couple a free-space beam to a set of waveguides

Then

we could automatically couple all the power to the one output guide

This could run continuously tracking changes in the beam

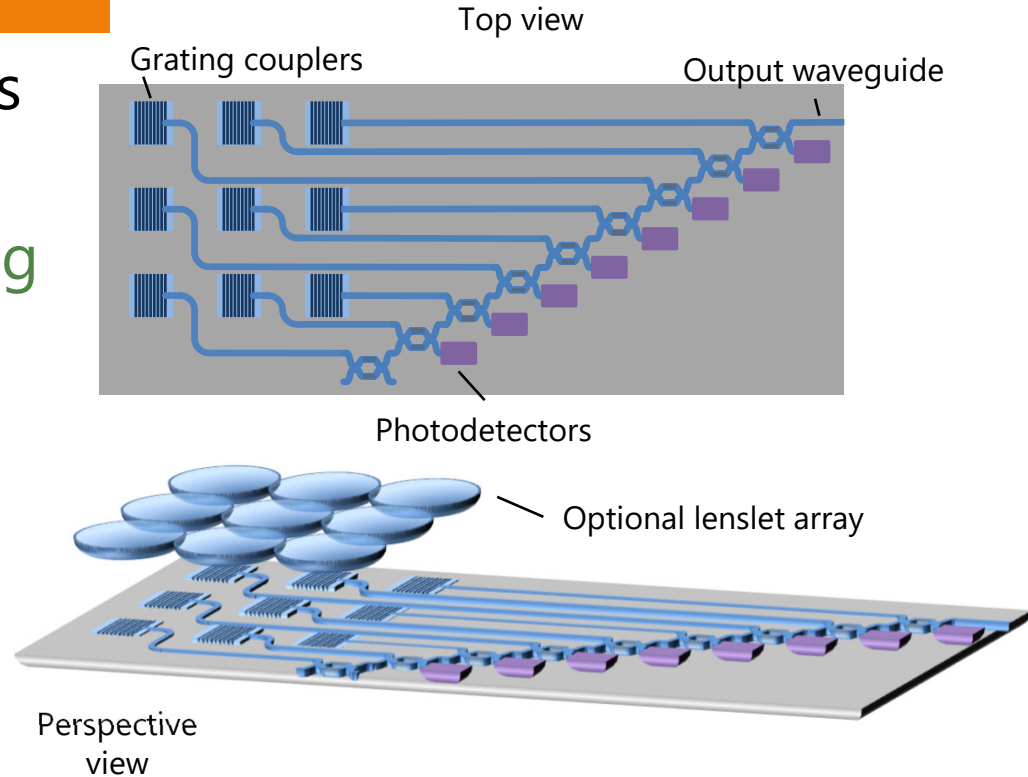


"Self-aligning universal beam coupler," Opt. Express **21**, 6360 (2013)

Self-aligning beam coupler

This has several different uses

- ❑ tracking an input source
 both in angle and focusing
- ❑ correcting for aberrations
- ❑ analyzing amplitude and phase of the components of a beam
- ❑ ...



"Self-aligning universal beam coupler," Opt. Express **21**, 6360 (2013)

"Diagonal line" self-aligning coupler

Note this works

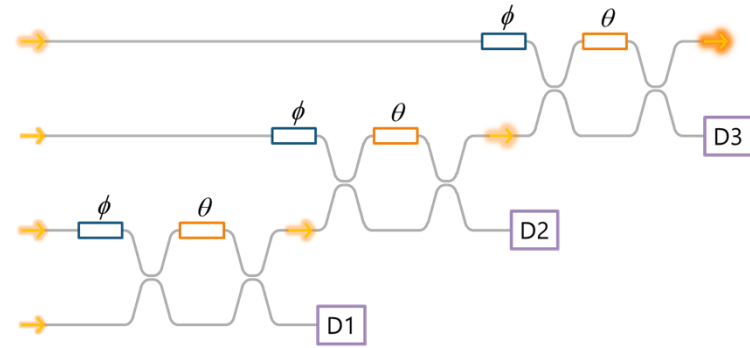
without calculations

without calibrations

The computation to set up this system

is physically performed by the system itself

which is nonlinear because of the feedback loops from detectors to phase shifters



"Self-aligning universal
beam coupler," Opt. Express
21, 6360 (2013)

“Diagonal line” self-aligning coupler

This kind of simple progressive algorithm
only works for certain topologies of
networks though

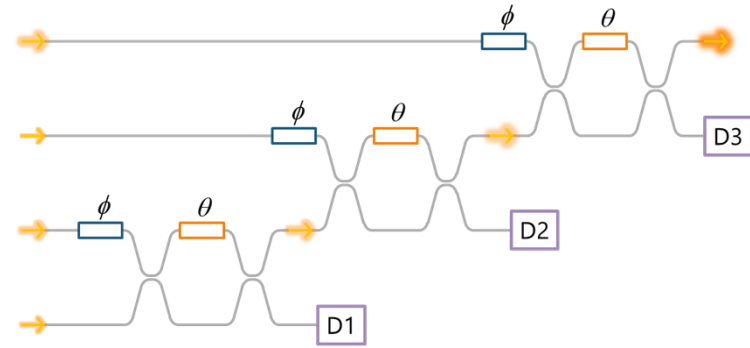
we understand this topology well

and it is a branch of graph theory

It is remarkable that we have a complex
nonlinear system

that nonetheless supports simple control
and configuration algorithms

that lead to stable and convergent
systems



“Self-aligning universal
beam coupler,” Opt. Express
21, 6360 (2013)

Some practical points about silicon photonic circuits

These silicon photonics circuits are typically made in foundries, such as
AMF, AIM, IMEC, ...

and many support multi-project wafers for university groups

Simple experimental circuits typically use small numbers of “ports”
e.g., 4, 9, 16

though circuits have been made with many hundreds of
interferometers

Phase shifting is typically done by heating up waveguide sections ~ 100
microns long

which takes milliwatts of power

Micromechanical phase shifters are under research and development
and would eliminate such powers

Such phase shifters have response times ~ milliseconds to microseconds

Faster phase shifters are possible

though they may be larger

Example early work on mesh optics

Early experimental mesh demonstrations

- J. Carolan, C. Harrold, C. Sparrow, E. Martín-López, N. J. Russell, J. W. Silverstone, P. J. Shadbolt, N. Matsuda, M. Oguma, M. Itoh, G. D. Marshall, M. G. Thompson, J. C. F. Matthews, T. Hashimoto, J. L. O'Brien, and A. Laing, "Universal linear optics," *Science* 349, 711-716 (2015)
- L. Zhuang, C. G. H. Roeloffzen, M. Hoekman, K.-J. Boller, and A. J. Lowery, "Programmable photonic signal processor chip for radiofrequency applications," *Optica* 2, 854-859 (2015)
- D. Pérez, I. Gasulla, J. Capmany, and R. A. Soref, "Reconfigurable lattice mesh designs for programmable photonic processors," *Opt. Express* 24, 12093-12106 (2016)
- Y. Shen, N. C. Harris, S. Skirlo, M. Prabhu, T. Baehr-Jones, M. Hochberg, X. Sun, S. Zhao, H. Larochelle, D. Englund, and M. Soljacic, "Deep Learning with Coherent Nanophotonic Circuits," *Nature Photonics* 11, 441-446 (2017)
- N. C. Harris, G. R. Steinbrecher, J. Mower, Y. Lahini, M. Prabhu, D. Bunandar, C. Chen, F. N. C. Wong, T. Baehr-Jones, M. Hochberg, S. Lloyd, and D. Englund, "Quantum transport simulations in a programmable nanophotonic processor," *Nature Photonics* 11, 447-452 (2017)

Self-configuring and self-correcting optics demonstrations

- A. Ribeiro, A. Ruocco, L. Vanacker, and W. Bogaerts, "Demonstration of a 4×4 -port universal linear circuit," *Optica* 3, 1348-1357 (2016)
- C. M. Wilkes, X. Qiang, J. Wang, R. Santagati, S. Paesani, X. Zhou, D. A. B. Miller, G. D. Marshall, M. G. Thompson, and J. L. O'Brien, "60 dB high-extinction auto-configured Mach-Zehnder interferometer," *Opt. Lett.* 41, 5318-5321 (2016)
- A. Annoni, E. Guglielmi, M. Carminati, G. Ferrari, M. Sampietro, D. A. B. Miller, A. Melloni, and F. Morichetti, "Unscrambling light – automatically undoing strong mixing between modes," *Light Science & Applications* 6, e17110 (2017)

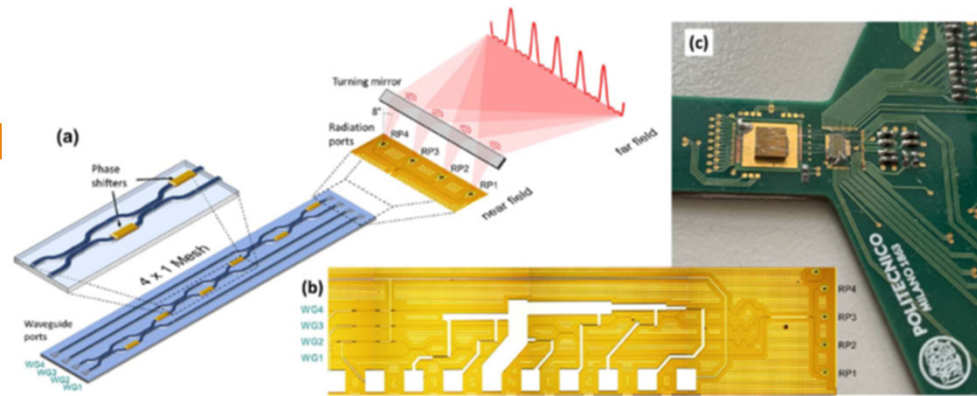
Theory of universal and self-configuring/correcting optics

- DM, "Self-aligning universal beam coupler," *Opt. Express* 21, 6360-6370 (2013)
- DM, "Self-configuring universal linear optical component," *Photon. Res.* 1, 1-15 (2013)
- DM, "Perfect optics with imperfect components," *Optica* 2, 747-750 (2015)

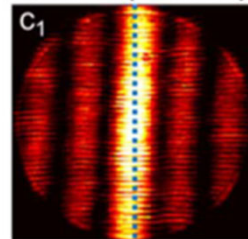
Pre-compensating a beam

Removing the effects of a diffusing mask with a mesh

1. optimize the mesh to maximize intensity in the center of the camera



No mask (mesh off)

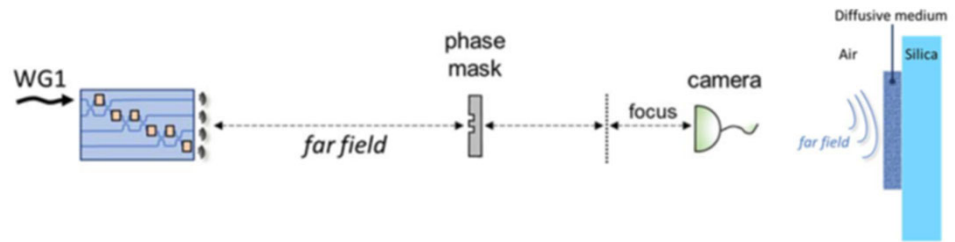
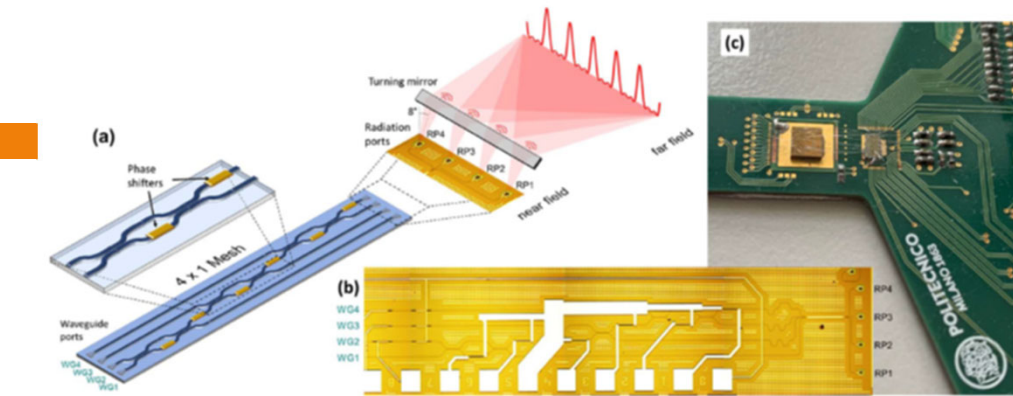


M. Milanizadeh, F. Toso, G. Ferrari, T. Jonuzi, D. A. B. Miller, A. Melloni, and F. Morichetti, "Coherent self-control of free-space optical beams with integrated silicon photonic meshes,". Photonics Research 9, 2196-2204 (2021)

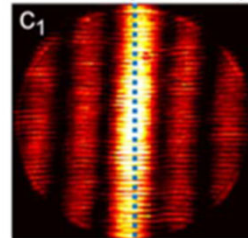
Pre-compensating a beam

Removing the effects of a diffusing mask with a mesh

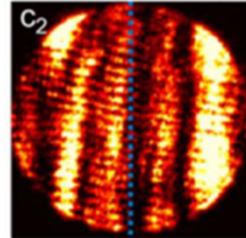
1. optimize the mesh to maximize intensity in the center of the camera
2. introduce a diffusing phase mask
3. re-optimize the mesh settings to restore the central maximum



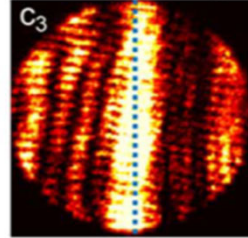
No mask (mesh off)



Mask (mesh off)



Mask (mesh on)



M. Milanizadeh, F. Toso, G. Ferrari, T. Jonuzi, D. A. B. Miller, A. Melloni, and F. Morichetti, "Coherent self-control of free-space optical beams with integrated silicon photonic meshes,". Photonics Research 9, 2196-2204 (2021)

Optimization methods

In addition to simple progressive algorithms

which work for certain architectures

and can be optimally fast

requiring the minimum possible number of measurements

other optimization approaches are possible

such as standard global optimization algorithms

and minimization approaches based on “dithering” individual phase shifters

Anecdotally, it appears that such optimization

both with progressive and global algorithms

can lead to good performance

even with imperfect components

e.g., imperfect split ratios in beamsplitters

A new kind of optics – separating
overlapping beams without
(fundamental) loss

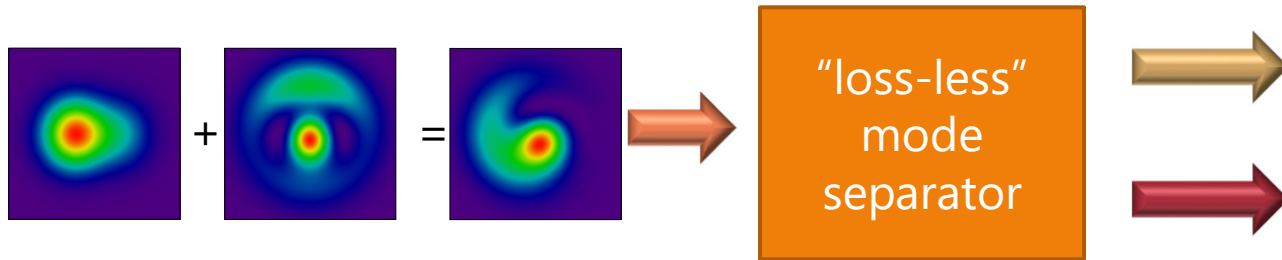
Example - Separating overlapping beams

In situations with

fixed

highly symmetric beams

there are good specific low-loss separation solutions



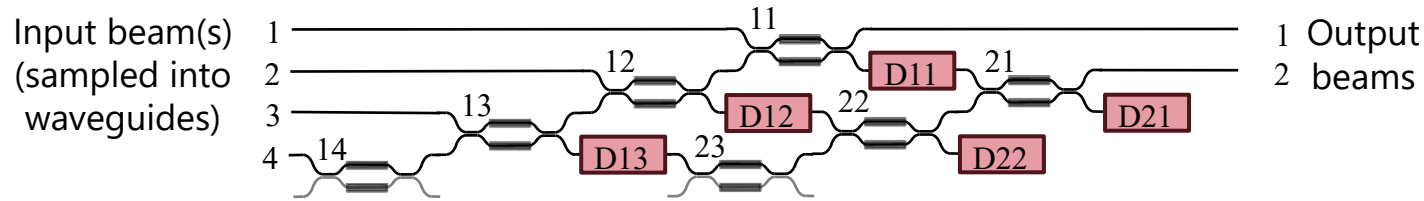
But for general cases

of lower symmetry and/or higher complexity

or where the beams change in time

general solutions have not been known

Separating multiple orthogonal beams



"Self-aligning universal beam coupler," Opt. Express **21**, 6360 (2013)

Once we have aligned beam 1 to output 1 using detectors D11 – D13
an orthogonal input beam 2 would pass entirely into the detectors
D11 – D13

If we make these detectors mostly transparent

this second beam would pass into the second diagonal "row"

where we self-align it to output 2 using detectors D21 – D22

separating two overlapping orthogonal beams to separate outputs

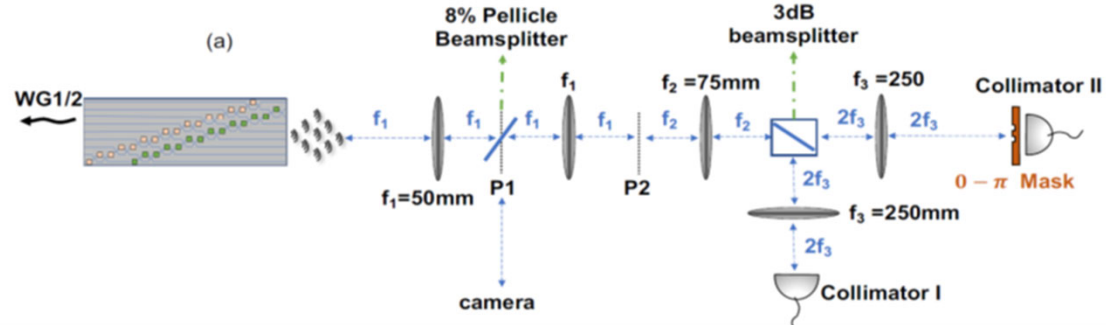
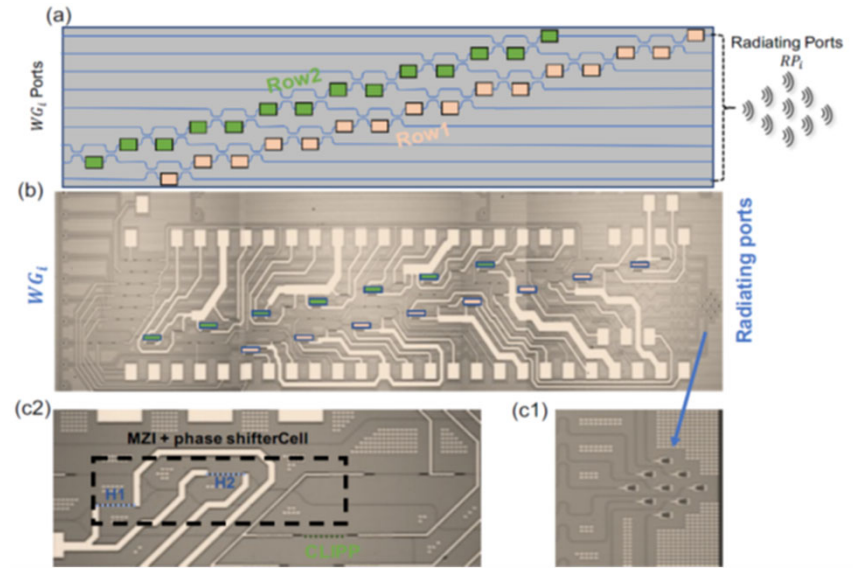
Separating free-space modes

9x2 diagonal line mesh

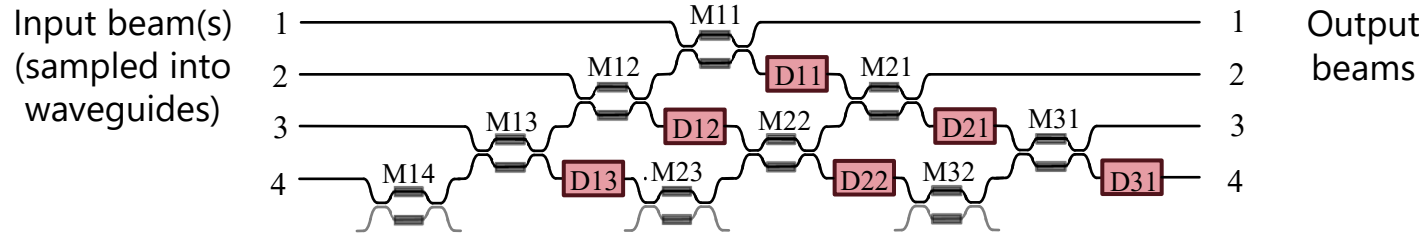
separates two orthogonal free-space input modes

automatically by self-configuration

M. Milanizadeh, SM. SeyedinNavadeh, F. Zanetto, V. Grimaldi, C. De Vita, C. Klitis, M. Sorel, G. Ferrari, D. A. B. Miller, A. Melloni, and F Morichetti, "Separating arbitrary free-space beams with an integrated photonic processor," Light: Science & Applications 11, 197 (2022)



Separating multiple orthogonal beams



"Self-aligning
universal beam
coupler," Opt.
Express **21**, 6360
(2013)

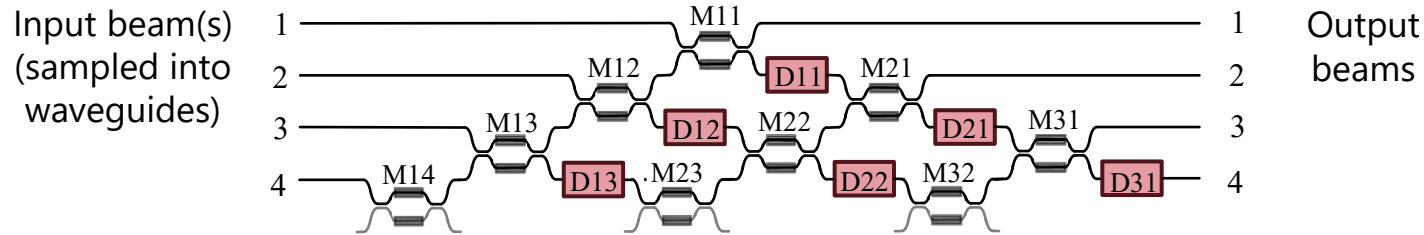
Adding more rows and self-alignments

separates a number of orthogonal beams

equal to the number of beam "segments", here, 4

Automatically undoing scattering
among multiple modes

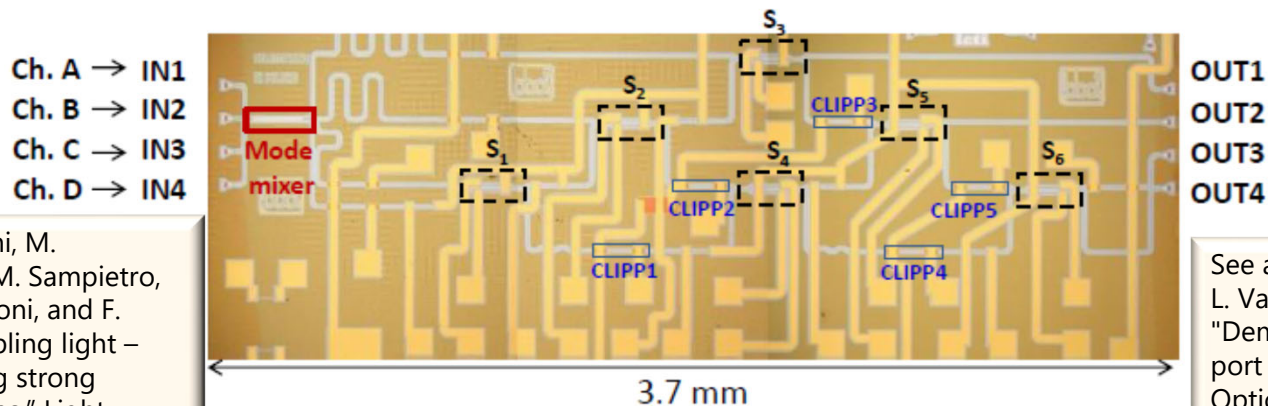
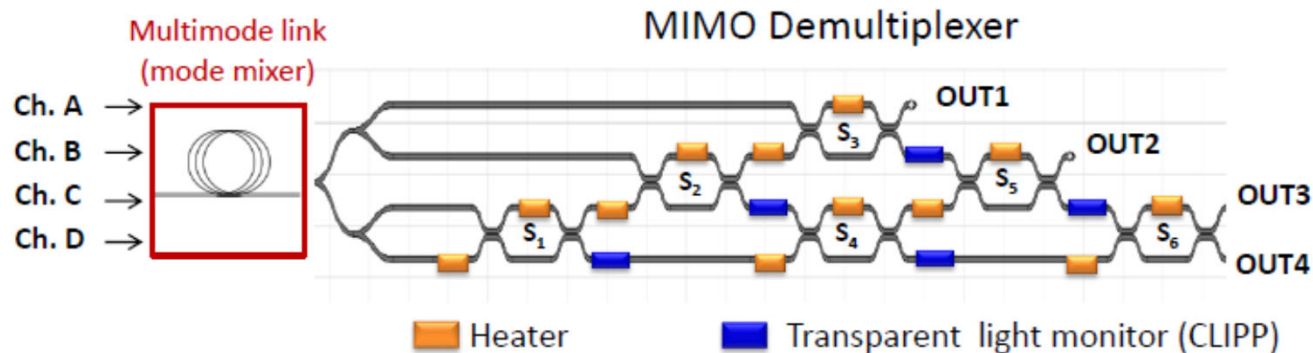
Separating multiple orthogonal beams



“Self-aligning
universal beam
coupler,” Opt.
Express **21**, 6360
(2013)

If we put identifying “tones” on each orthogonal input “beam”
and have the corresponding diagonal row of detectors look for that tone
then the mesh can continually adapt to the orthogonal inputs
even when they are all present at the same time
and even if they change

Integrated MIMO demultiplexer: technology



A. Annoni, E. Guglielmi, M. Carminati, G. Ferrari, M. Sampietro, D. A. B. Miller, A. Melloni, and F. Morichetti, "Unscrambling light – automatically undoing strong mixing between modes," *Light Science & Applications* 6, e17110 (2017)

See also A. Ribeiro, A. Ruocco, L. Vanacker, and W. Bogaerts, "Demonstration of a 4 × 4-port universal linear circuit," *Optica* 3, 1348-1357 (2016)

- Transparent detectors required for sequential tuning
- CLIPP-assisted circuit reconfiguration & feedback control

Speed of mesh self-configuration

This analysis

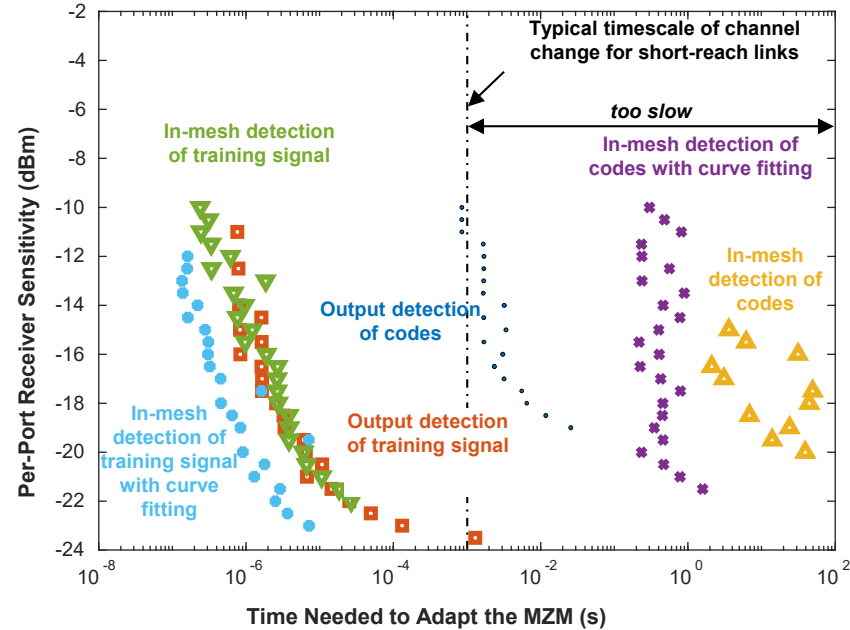
comparing several minor variants of the detection approach

shows that, even with only 10's of microwatts of input powers

entire networks (e.g., 4x4) can self-configure in microseconds or less

So, fast enough for

- km-scale multimode fiber optics
- free-space turbulence compensation
- rapid configuration for mathematical problems



K. Choutagunta, I. Roberts, D. A. B. Miller, and J. M. Kahn, "Adapting Mach-Zehnder Mesh Equalizers in Direct-Detection Mode-Division-Multiplexed Links," J. Lightwave Technol. 38, 723 (2020)

Topology of mesh architectures

Mathematics and meshes

Different mathematical concepts

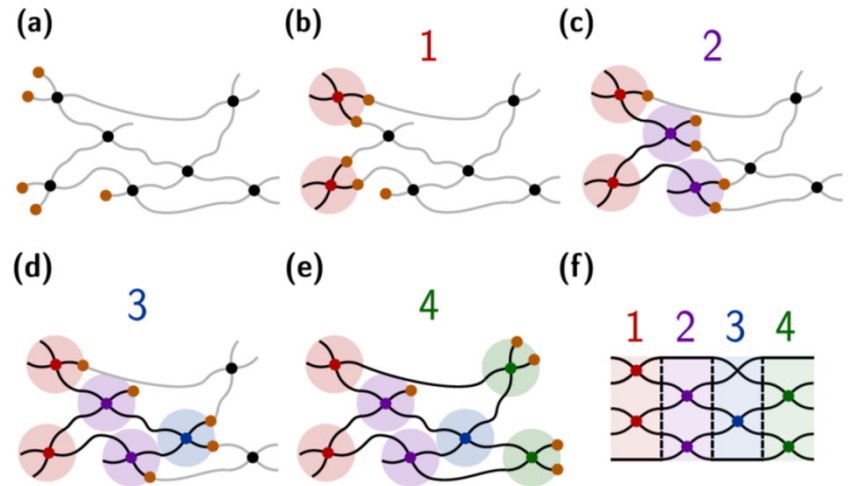
such as graph theory

are starting to appear in discussions of optics

e.g., directed acyclic graphs

which correspond to "forward-only" circuits

See also X. Chen et al, "Graph representations for programmable photonic circuits," J. Lightwave Technol. 38, 4009 (2020)

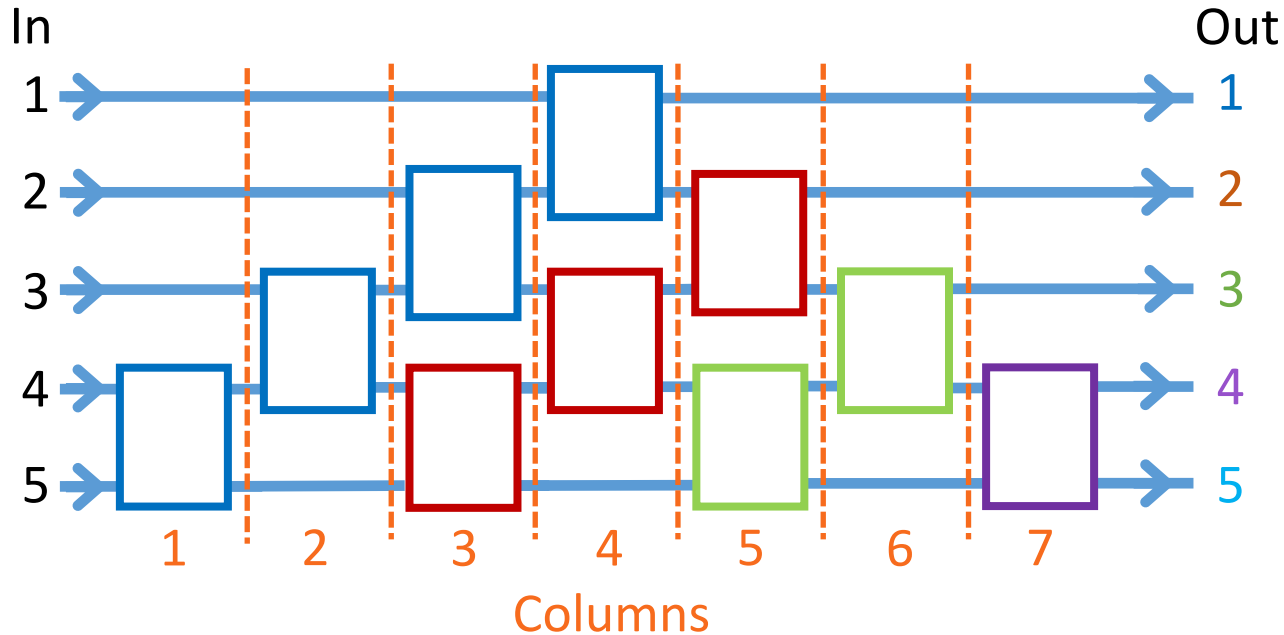


Topological sorting of an optical network into columns for parallel configuration

S. Pai et al., "Parallel programming of an arbitrary feedforward photonic network," IEEE J. Sel. Top. Quantum Electron. 25, 6100813 (2020)

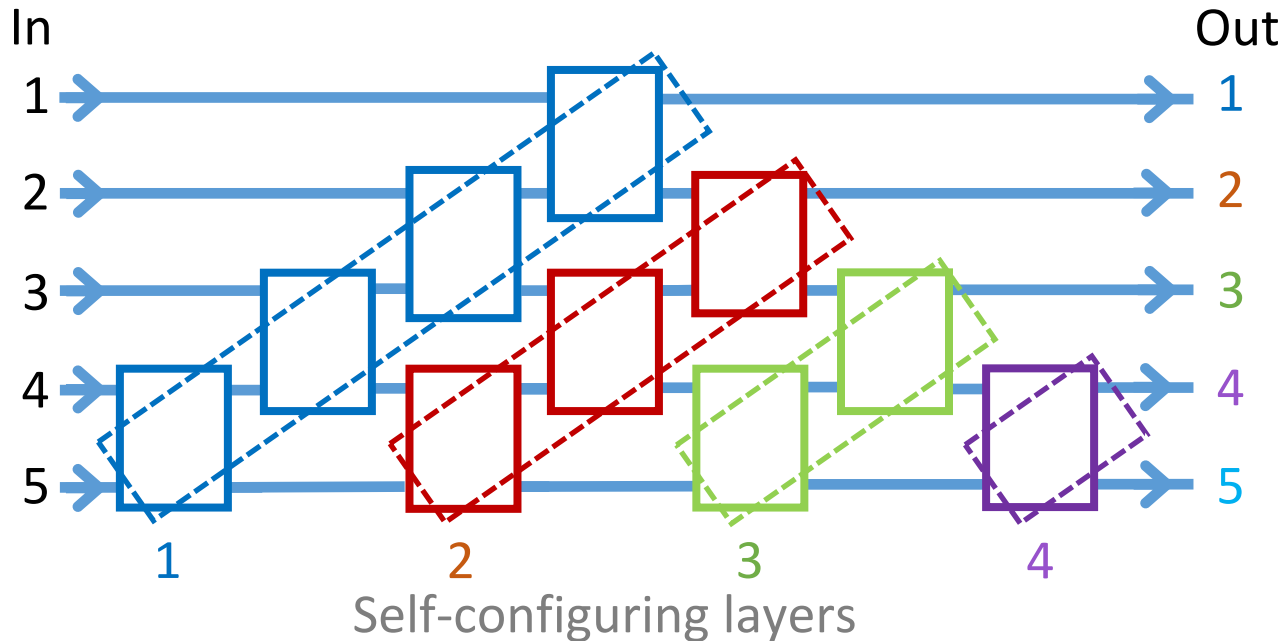
Column topology

“Columns” can be identified with a simple topological algorithm and configured or calibrated in parallel



Self-configuring layer topology

“Self-configuring layers” have one connection path through 2x2 blocks from their output to each of their inputs



Applications of self-configuring mesh circuits

Other applications and extensions

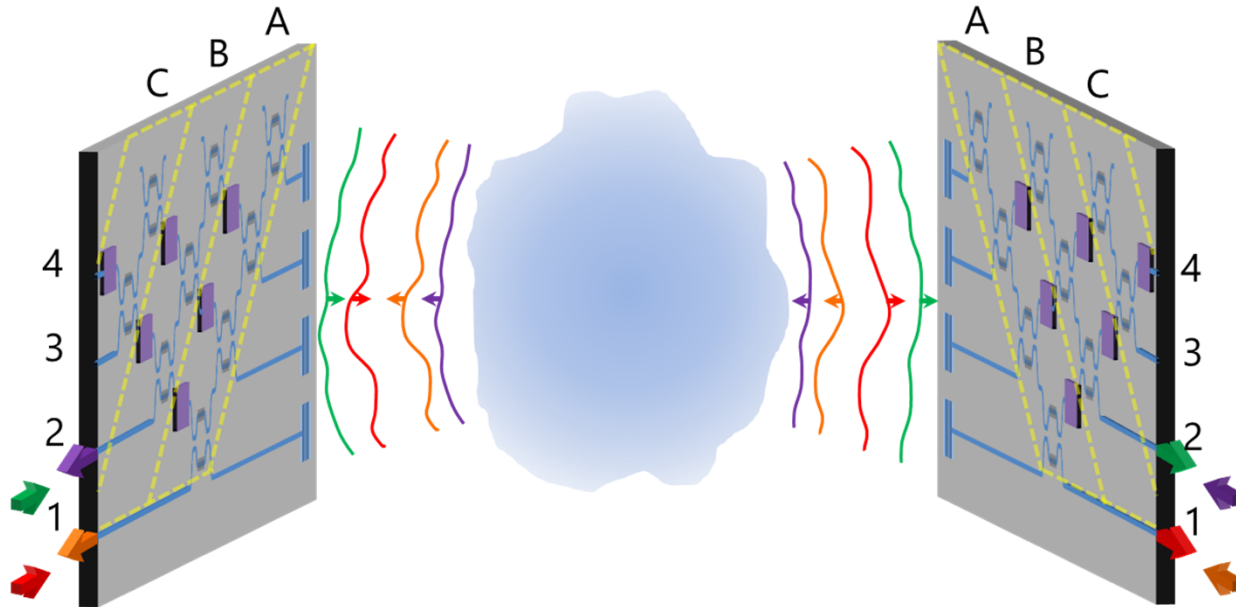
- ❑ phase conjugation
- ❑ undoing scattering
 - including potential real-time self-configuration
 - e.g., for undoing atmospheric turbulence or mode scattering in fibers
- ❑ finding the best channels for communications
- ❑ self-calibrating, self-correcting and self-stabilizing complex optical systems

Establishing optimum orthogonal channels

Iterating back and forward between the two sides

finds the optimal orthogonal channels through any scatterer

from the waveguides on the left to the waveguides on the right



"Establishing optimal wave communication channels automatically," J. Lightwave Technol. 31, 3987 (2013)

Establishing optimum orthogonal channels - experiment

System of two “facing” meshes

through simple optics

These can be misaligned

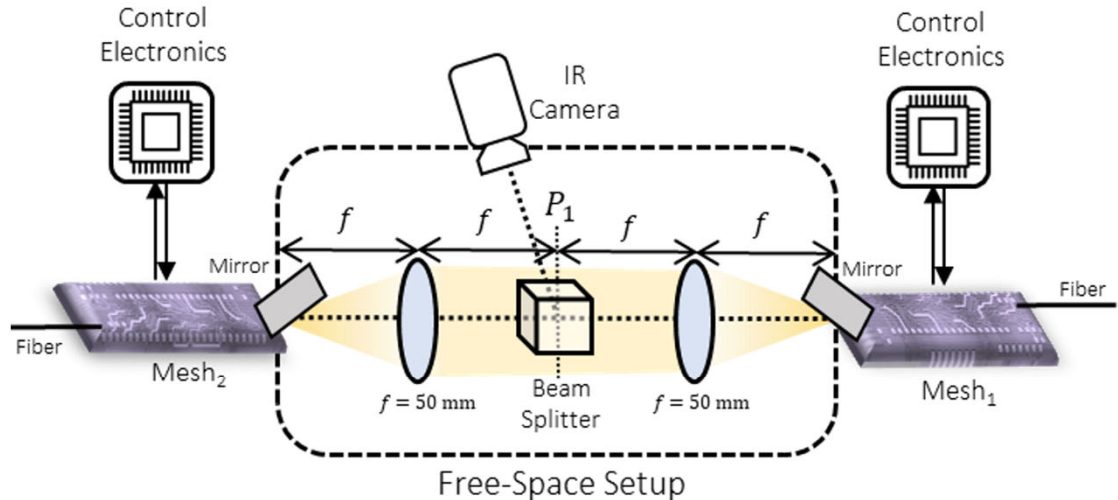
and we can introduce

aberrations or

partial blocking

in the path

The system still self-aligns to find the best, orthogonal channels

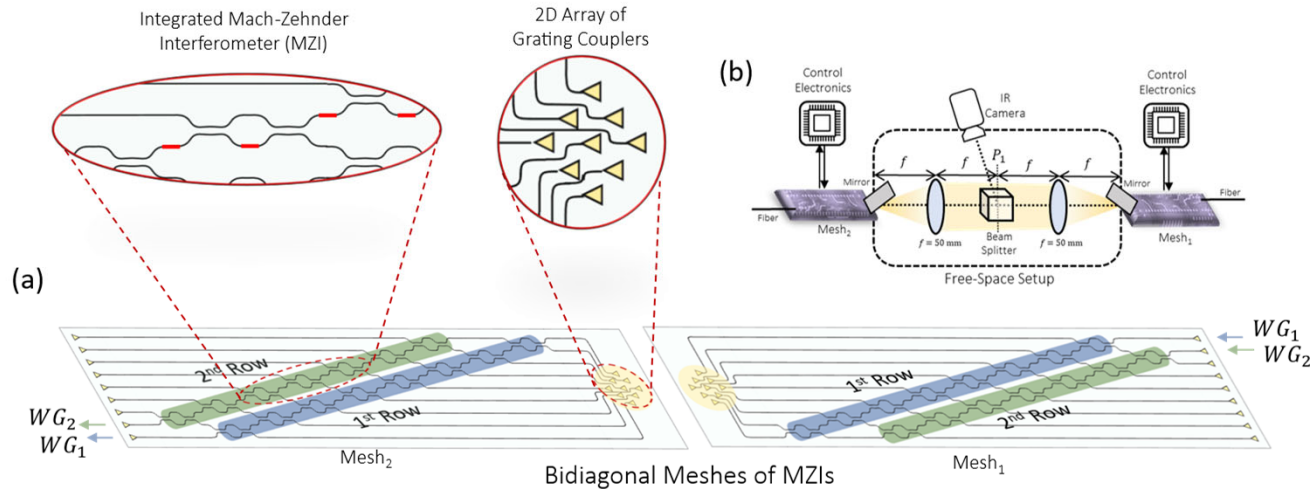


SM SeyedinNavadeh, M Milanizadeh, F Zanetto, V Grimaldi, C De Vita, G Ferrari, D A B Miller, A Melloni, F Morichetti, “Multi-channel free-space optical communication between self-configuring silicon photonic meshes”, ECIO22, 4-6 May 2022, Milan, Italy, Paper F.E.2

Establishing optimum orthogonal channels - experiment

Two "9x2" meshes allow automatic self-configuration

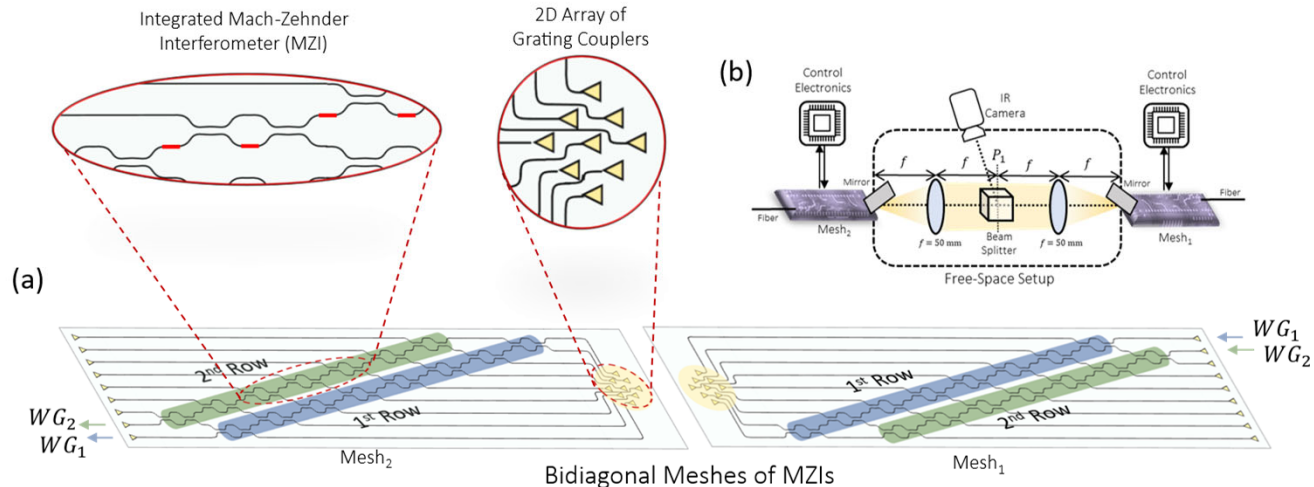
signals in WG1 on the right can automatically be aligned to appear out of WG1 on the left, and, at the same time
signals in WG2 on the right can automatically be aligned to appear out of WG2 on the left



Establishing optimum orthogonal channels - experiment

Even after inserting a partially blocking mask in the optical path between the meshes

the system can re-establish orthogonal channels automatically
with > 30 dB rejection between the channels



Arbitrary beam generation and analysis

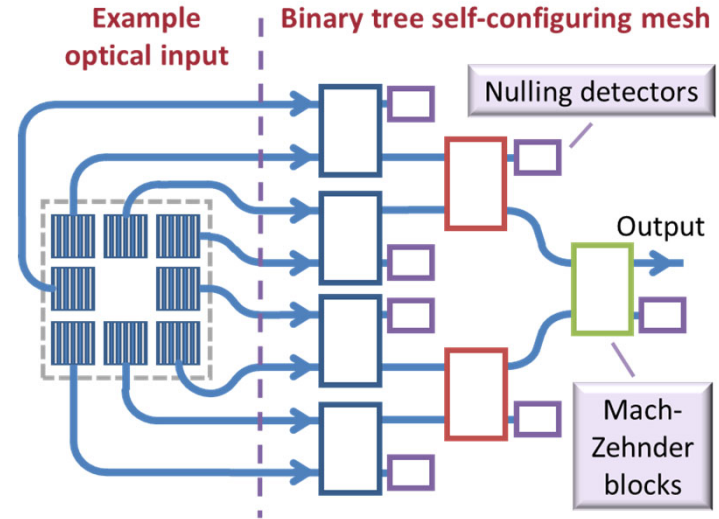
Automatically analyze an arbitrary input beam

full amplitude and phase

by self-aligning a mesh

and calculating from the resulting
settings

Generate an arbitrary beam by running this
network backwards



D. A. B. Miller, "Analyzing and generating multimode optical fields using self-configuring networks," *Optica* 7, 794-801 (2020)

See also J. Bütow, J. S. Eismann, M. Milanizadeh, F. Morichetti, A. Melloni, D. A. B. Miller, and P. Banzer, "Spatially resolving amplitude and phase of light with a reconfigurable photonic integrated circuit," *Optica* 9, 939-946 (2022)

Universal matrix multiplier chip

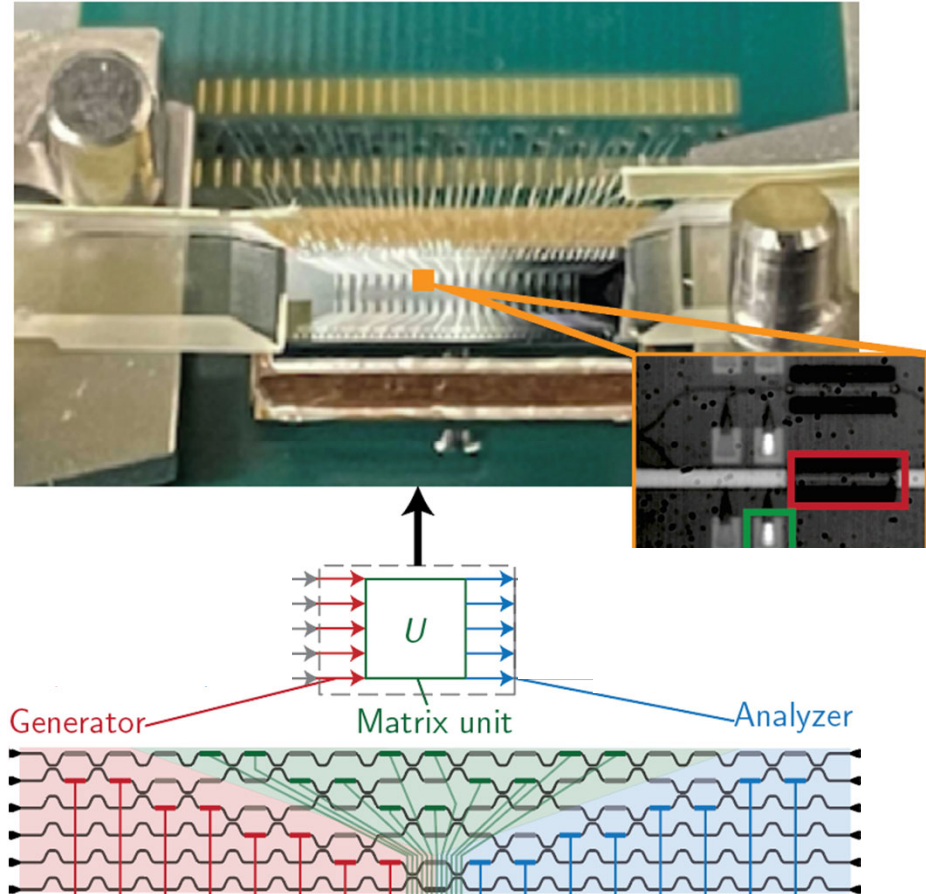
Universal and matrix multiplying chip

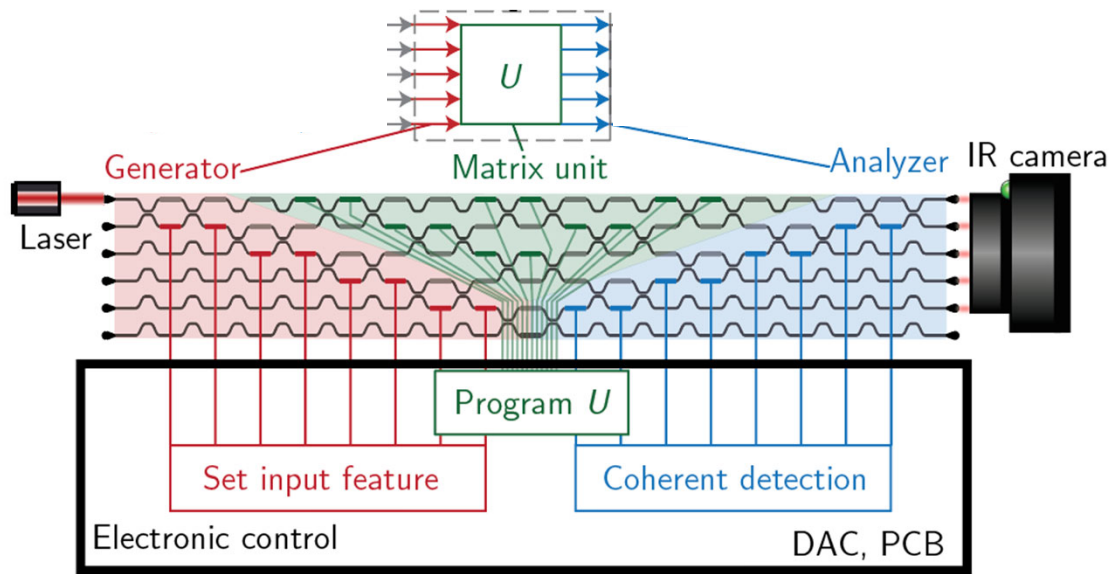
4x4 unitary Mach-Zehnder mesh with

- monitors at every MZI output and on every MZI "arm"
- "generator" to create any complex input vector
- and "analyzer" to measure the complex output vector
- also allows full phase measurement from input to output

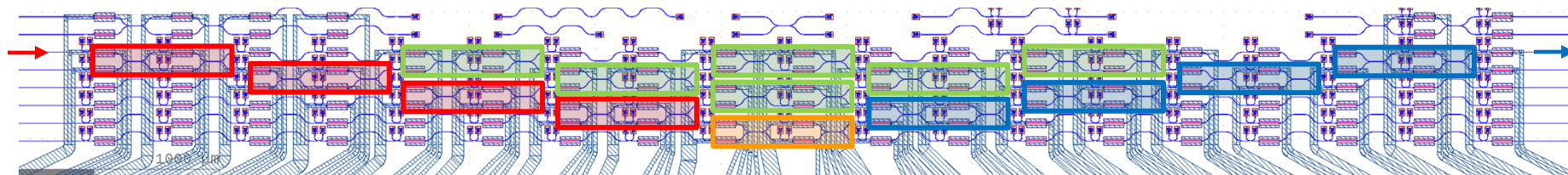
Note this design can keep all interferometric processes on chip

only an external input light source and final measuring power detectors are off-chip





Matrix unit



Vector generator

Vector analyzer

Universal matrix multiplier chip

Full complex matrix multiplication

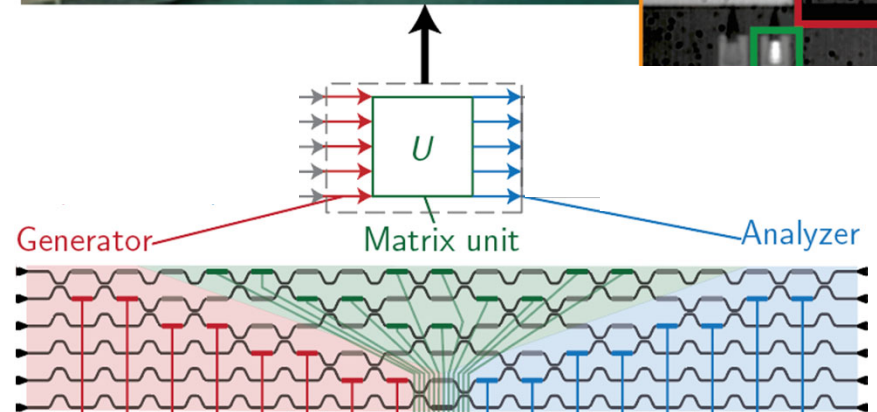
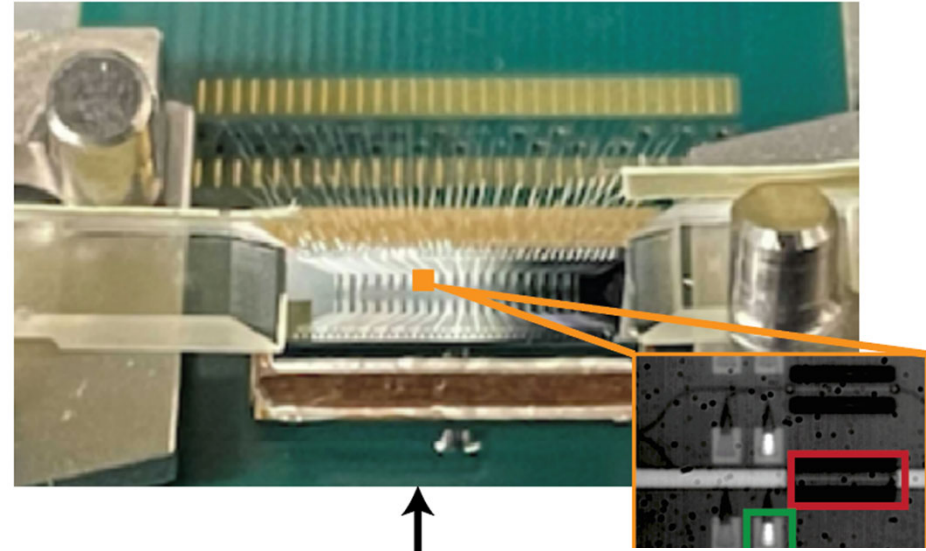
with vector generation and vector analysis

Photonic back-propagation neural net training

S. Pai, Z. Sun, T. W. Hughes, T. Park, B. Bartlett, I. A. D. Williamson, M. Minkov, M. Milanizadeh, N. Abebe, F. Morichetti, A. Melloni, S. Fan, O. Solgaard, and D. A. B. Miller, "Experimentally realized in situ backpropagation for deep learning in nanophotonic neural networks," DOI: 10.48550/arXiv.2205.08501

Digital matrix multiplication for cryptography

S. Pai, T. Park, M. Ball, B. Penkovsky, M. Milanizadeh, M. Dubrovsky, N. Abebe, F. Morichetti, A. Melloni, S. Fan, O. Solgaard, and D. A. B. Miller "Experimental evaluation of digitally-verifiable photonic computing for blockchain and cryptocurrency," DOI: 10.48550/arXiv.2205.08512



Other applications and extensions

- ❑ mathematical equation solving
- ❑ linear optical quantum circuits
- ❑ optical neural networks
- ❑ r.f. photonics
- ❑ new ways of sensing where we look for the features we want, and can adapt and program those to the application
 - "superpixels"
 - e.g., microscopy



Universal self-configuring architectures

Universal self-configuring photonics

Universal architectures

e.g., based on singular value decomposition (SVD)

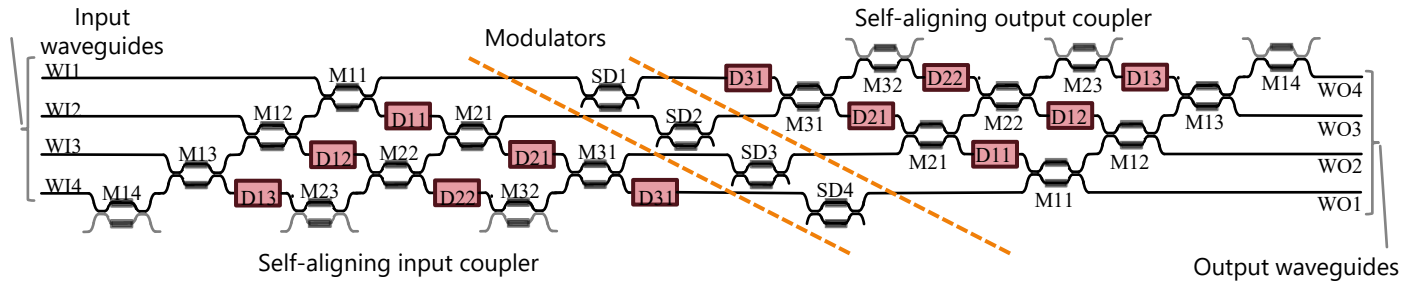
allow any matrix multiplication

for arbitrary linear optics, neural networks, classical or quantum processing

and can be self-configured

and hence offer universal field-programmable linear arrays

General multiple mode converter



"Self-configuring
universal linear
optical component,"
Photon. Res. **1**, 1
(2013)

The self-aligning input coupler mesh on the left can couple any four orthogonal inputs

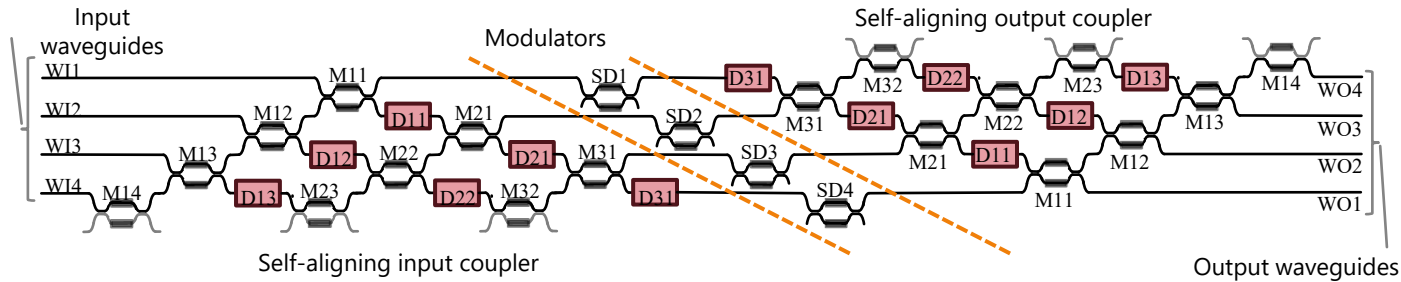
each to different single waveguides in the middle

Light in those single waveguides can be converted into any other set of four orthogonal outputs on the right

by the self-aligning output coupler mesh on the right

The amplitude and phase of this conversion can be controlled by the line of modulators in the middle

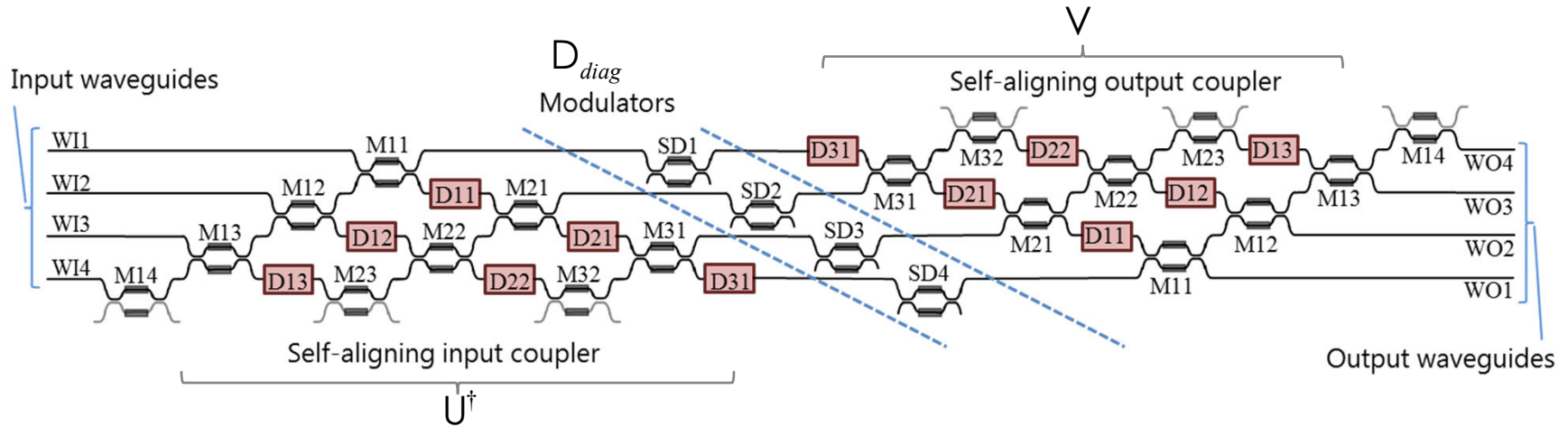
General multiple mode converter



"Self-configuring universal linear optical component,"
Photon. Res. **1**, 1
(2013)

This kind of universal mode conversion, with such modulation
corresponds to being able to implement
an arbitrary (and non-unitary) matrix with such a mesh (at least if
we do not require gain)
so this mesh is fully universal for performing any linear
transformation

General multiple mode converter



The mathematical reason why this works is because

we can always perform the “singular value decomposition” of a matrix

which means a matrix D can always be written in the form

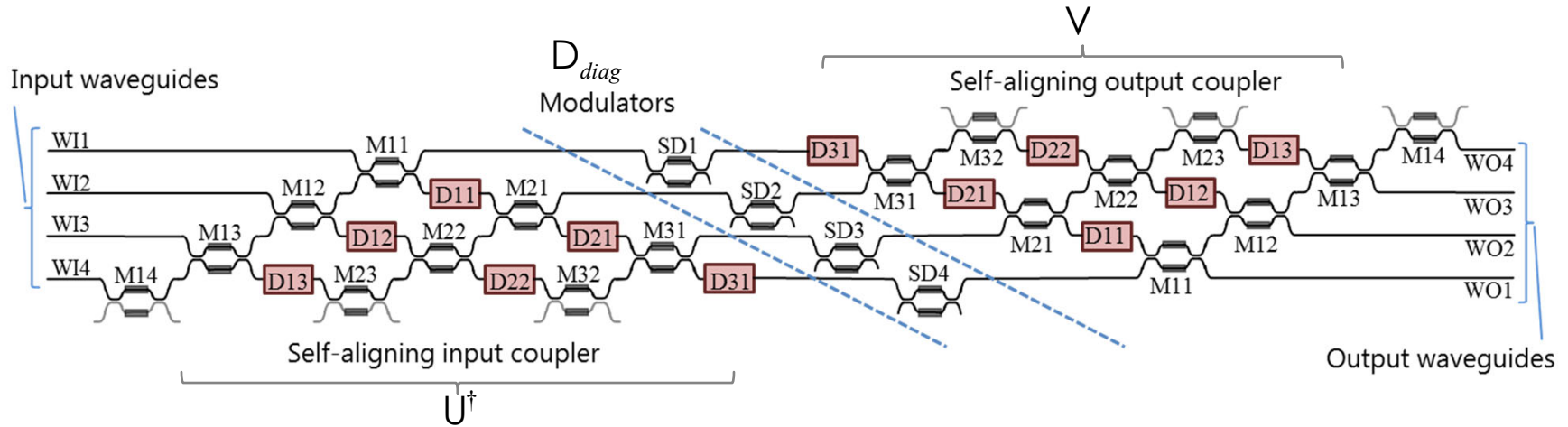
$$D = VD_{diag}U^\dagger$$

where U and V are “unitary” (lossless) matrices

and D_{diag} is a diagonal matrix

“Self-configuring
universal linear
optical component,”
Photon. Res. **1**, 1
(2013)

General multiple mode converter



The optical "units" in the mesh implement the singular value decomposition $D = VD_{diag}U^\dagger$

This is the first proof that any linear optical component is possible
and that any linear optical system can be factored into a set of
2-beam interferences

This can be used in thought experiments for fundamental proofs

"Self-configuring
universal linear
optical component,"
Photon. Res. **1**, 1
(2013)

Waves, modes, and optics –
viewing linear optics through
singular-value decomposition

Decomposing optical systems

We can also flip this logic around

We can always perform the singular value decomposition of an optical component or system

So any linear optical system can be described as a mode-converter

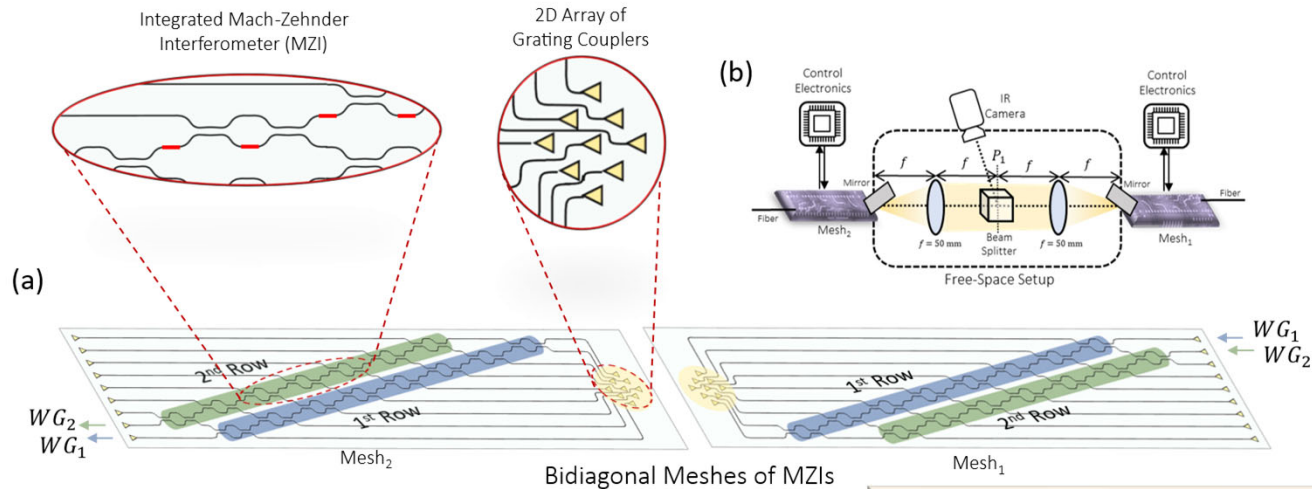
Opt. Express **20**, 23985 (2012)

These sets of modes turn out to have basic physical significance

Adv. Opt. Photon. 11, 679 (2019)

Establishing optimum orthogonal channels - experiment

The system of two “facing” chips is performing the singular-value decomposition of the optics, here for two channels, between the inputs to the grating couplers on one side and the outputs from the grating couplers on the other side establishing the “communication modes” in the system



Waves, modes, communications and optics

For any linear optical system

singular value decomposition gives

an optimal, orthogonal set of “input” functions that map, one-by-one, to an optimal orthogonal set of “output” functions

“Waves, modes, communications and optics”
Adv. Opt. Photon. 11, 679-825 (2019)

These allow

- ❑ A rigorous “communications mode” counting of communications channels including the conclusion that there is always a finite number of usable channels
 - including specific new limits for various optical systems
- ❑ A general form of diffraction theory, valid for all sizes and shapes of objects
- ❑ The most economical “mode-converter basis” description of any linear optics
- ❑ New versions of Kirchhoff’s radiation laws, valid for all objects
 - including nanophotonics and non-reciprocal systems ...
- ❑ A new, “mode by mode” version of Einstein’s A & B coefficient argument
- ❑ A new quantization of the radiation field in any volume

Conclusions

Conclusions

For a copy of these viewgraphs,
please e-mail dabm@stanford.edu

Self-configuring photonics enables complex circuits for new optics

The algorithms to calibrate and use these circuits are

simple and fast

The many uses of these ideas are just starting

These ideas also complement a fundamentally new way of looking
at optics

**the “communications modes” and “mode-converter basis sets”
from singular value decomposition**

Funding from

Air Force Office of Scientific Research FA9550-17-1-0002 and FA9550-21-1-0312

European Commission through the H2020 project SuperPixels (grant 829116)

Part of this work was carried out at Polifab, Politecnico di Milano, Milan, Italy

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